

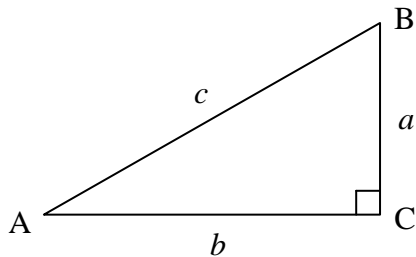
**Worksheet 1-1: Trigonometric Ratios**

The relationships between the acute angles and the sides of a right triangle are expressed in terms of **trigonometric ratios**. The three primary trigonometric ratios are **sine** ratio (sin), **cosine** ratio (cos), and **tangent** ratio (tan).

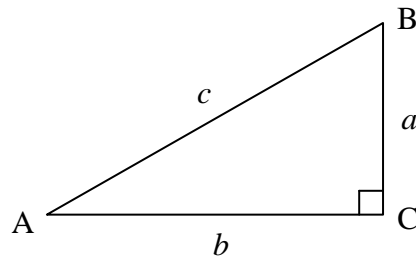
A **right triangle** is a triangle with a 90° right angle and two acute angles (less than 90°). The longest side opposite to the right angle is called the **hypotenuse** and the other two shorter sides are called the **legs**.

**SOH CAH TOA:**

For ∠A :



For ∠B :



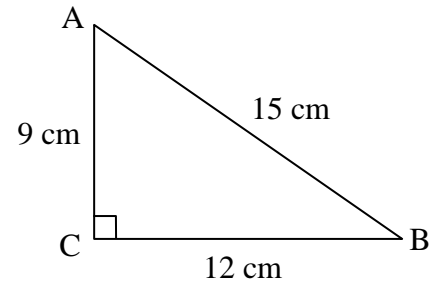
**Note:** The legs of a right triangle are labelled as opposite or adjacent relative to the acute angle of interest. They are different for different acute angles. So, first identify the acute angle of interest; then label the respective sides accordingly.

$\sin A = \frac{\textit{Opposite}}{\textit{Hypotenuse}} = \text{---} = \text{---}$ $\cos A = \frac{\textit{Adjacent}}{\textit{Hypotenuse}} = \text{---} = \text{---}$ $\tan A = \frac{\textit{Opposite}}{\textit{Adjacent}} = \text{---} = \text{---}$	$\sin B = \frac{\textit{Opposite}}{\textit{Hypotenuse}} = \text{---} = \text{---}$ $\cos B = \frac{\textit{Adjacent}}{\textit{Hypotenuse}} = \text{---} = \text{---}$ $\tan B = \frac{\textit{Opposite}}{\textit{Adjacent}} = \text{---} = \text{---}$
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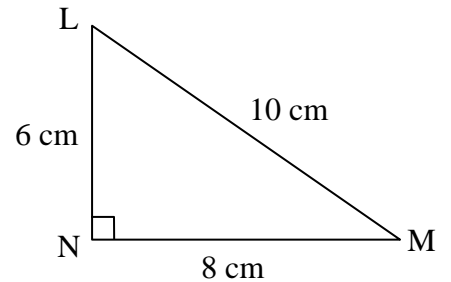
**Using a Calculator:**

<p><b>Scientific Calculator</b> Find the value of a trigonometric ratio: sin 40° = ? Press <b>40</b> <input type="button" value="SIN"/> <input type="button" value="="/></p> <p>Find the measure of an angle: sin A = 0.5, ∠A = ? Press <b>0.5</b> <input type="button" value="2&lt;sup&gt;nd&lt;/sup&gt;"/> <input type="button" value="SIN"/> <input type="button" value="="/></p>	<p><b>DAL Calculator</b> Find the value of a trigonometric ratio: sin 40° = ? Press <input type="button" value="SIN"/> <b>40</b> <input type="button" value="="/></p> <p>Find the measure of an angle: sin A = 0.5, ∠A = ? Press <input type="button" value="2&lt;sup&gt;nd&lt;/sup&gt;"/> <input type="button" value="SIN"/> <b>0.5</b> <input type="button" value="="/></p>
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1. For  $\triangle ABC$ , find the three primary trigonometric ratios for  $\angle A$ .  
Express each answer as a fraction in lowest terms.



2. For  $\triangle LMN$ , find the three primary trigonometric ratios for  $\angle M$ .  
Express each answer as a fraction in lowest terms.



3. Evaluate each trigonometric ratio. Round your answers to four decimal places.

(a)  $\sin 40^\circ$

(b)  $\cos 50^\circ$

(c)  $\tan 60^\circ$

(d)  $\sin 35^\circ$

(e)  $\cos 25^\circ$

(f)  $\tan 87^\circ$

4. Find the measure of each angle, to the nearest tenth of a degree.

(a)  $\cos A = 0.6789$

(b)  $\sin B = 0.829$

(c)  $\tan C = 3.7321$

(d)  $\cos X = 0.3907$

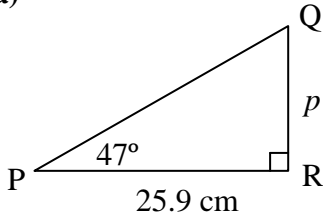
(e)  $\sin Y = 0.8197$

(f)  $\tan Z = 0.5789$

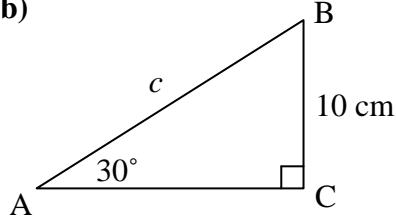
**Find the Length of a Side:**

5. Find each side length, to the nearest tenth of a centimetre.

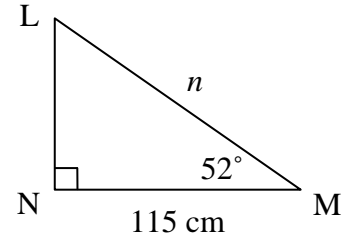
(a)



(b)



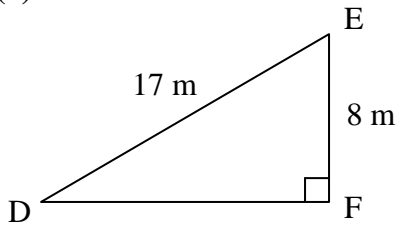
(c)



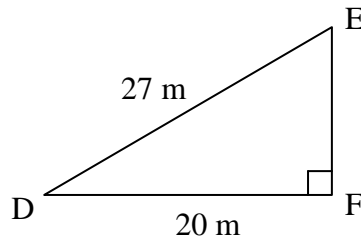
**Find an Angle Given the Length of Two Sides:**

6. Find the measure of  $\angle D$  to the nearest degree.

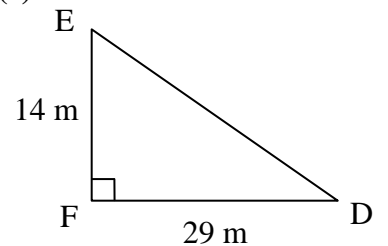
(a)



(b)



(c)



**Answers:** 1.  $\sin A = \frac{4}{5}$ ,  $\cos A = \frac{3}{5}$ ,  $\tan A = \frac{4}{3}$ ; 2.  $\sin M = \frac{3}{5}$ ,  $\cos M = \frac{4}{5}$ ,  $\tan M = \frac{3}{4}$ ;

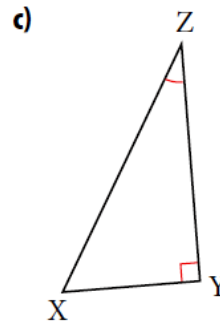
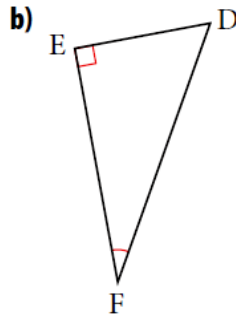
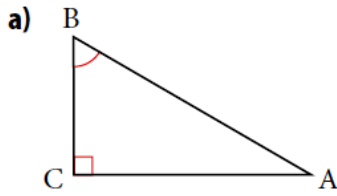
3. (a) 0.6428, (b) 0.6428, (c) 1.7321, (d) 0.5736, (e) 0.9063, (f) 19.0811;

4. (a)  $47.2^\circ$ , (b)  $56^\circ$ , (c)  $75^\circ$ , (d)  $67^\circ$ , (e)  $55.1^\circ$ , (f)  $30.1^\circ$ ; 5. (a) 27.8 cm, (b) 20 cm, (c) 186.8 cm;

6. (a)  $28^\circ$ , (b)  $42^\circ$ , (c)  $26^\circ$ .

**Practise**

1. Name the opposite, adjacent, and hypotenuse sides associated with  $\angle B$ ,  $\angle F$ , and  $\angle Z$ .



2. Evaluate. Round your answers to four decimal places.

a)  $\sin 30^\circ$

b)  $\cos 45^\circ$

c)  $\tan 60^\circ$

3. Find the measure of each angle to the nearest tenth of a degree.

a)  $\sin A = 0.2345$

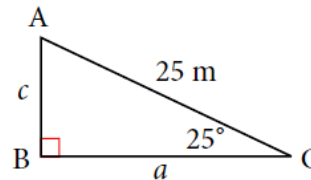
b)  $\cos B = 0.8765$

c)  $\tan C = 1.2345$

4. a) Find the measure of side  $a$  to the nearest metre.

b) Find the measure of side  $c$  to the nearest metre.

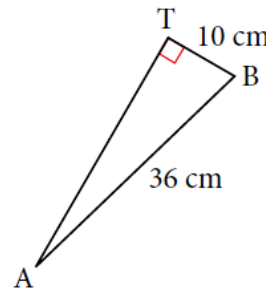
c) Find the measure of  $\angle A$ .



5. a) Find the measure of  $\angle A$  to the nearest tenth of a degree.

b) Find the measure of  $\angle B$  to the nearest tenth of a degree.

c) Find the measure of side  $b$  to the nearest centimetre.



**Answers**

1. a) opposite: AC or  $b$ ; adjacent: BC or  $a$ ; hypotenuse: AB or  $c$

b) opposite: DE or  $f$ ; adjacent: EF or  $d$ ; hypotenuse: DF or  $e$

c) opposite: XY or  $z$ ; adjacent: YZ or  $x$ ; hypotenuse: XZ or  $y$

2. a) 0.5000

b) 0.7071

c) 1.7321

3. a)  $\angle A = 13.6^\circ$

b)  $\angle B = 28.8^\circ$

c)  $\angle C = 51.0^\circ$

4. a) 23 m

b) 11 m

c)  $65^\circ$

5. a)  $16.1^\circ$

b)  $73.9^\circ$

c) 35 cm